When payables are given shows of an action is delimined by chaine of a prob, dist. (To say you know A's probes and you know his VN payoffs - A may be you - is to say you know what he wants to choose. To say you know what he wants to choose is to say you know his (max) expectation; from which payoffs and/or probe can be inferred (Why bother?) if you know other things). So the choice of a prob dist by a committee - or by a person meto finds severable prob dists reasonable and has no definite reasons to regard one as now likely than another or as equally likely, or was is not confident of his reasons - in a decision problem, each 3 (chat) having payoffs companding to the expected value of the "best" action who that action dist for each of the other "wasorable" diets. Thirthold problems; several of the 3's in question may give the same ordering or the same aftimen, or may order certain actions the same way but not athers; disagrument our actions is constrained by disagrument over disto, but not in one-one fashion; it is not musey to wach total agruent on dist. to arrive at action

i.e. many rows in matrix below are identical and all but ? one can be dignored: 3, 3, 3, ... X(3,) is aptimen & in original S, E X(3), dieraion problem w. r.t. E, 3, Ex(3,) Inagene choice committee made up into two subcommittees; Payoffs (Policy) and Proles (Intelligence). 1) Bayes approach implies these committees whach conclusions suporately on suparate data, turn own results to Decision-maker (Pres, NSC, Ops); or, Probo turn our results to Palicy, which they produces unique chaice (results in form of a single prot, dist). 2) Minimal right implies that Policy committee arrives it would ignoring Probs conclusions, just because they dishit agas totally. Why should 3) How should Probe committee respect its findings and disagreement? our

Why should Brobs conmittee uport its degree of uncertainty or range of possibilities, except in prot. tuno? (as RAND says). (Ono: became & may want to give different weight to different "possibilities" - prob disto - defending on payoffo, the aiselt of Policy Connetter. So Intell should note 2 sonts of findings 2) ambiguit, ourall adequary of info b) Relative hikelehoods, of wents and of prob. disto. of (3) shows high ambiguity, D will want to make judgement of p and & introd of just turning own (6) to Policy Committee. finding out objective consequence of actions & wents, butill belief on producting there, is addition to producting onlesse probe of wint).

Military arganization The effective of a military system must showings be judged in the light of a number of degradation-contingencies. a sugrant is gudged not only on low well his platton performs but on hour de runs it; sperificilly on (a) hour will it performs under his direction and (6) how will it would perform without him (of he were tilled, out of comm, replaced. aside from the problem of training subordinates for Madership positions (which could be done separately) phatoon must be trained of run to operate will without comes and without normal brokership, Still with platon this mainly amounts to clinity to carry out a given decision, task; ability to be ne-directed is less important.

The difference between maximin and minimax-betwen the values of the minorant and majorant games-is the least amount a player could gain by "finding out" the enemy-estimating his intentions correctly. In a normalized game, where the enemy doesn't know he will be found out, the actual gain might be much more: from maximin to maximax.

But even the minimum gain might be significant, if it is greater than zero. If opponent uses mixed strat, it would be zero. BUT: if there is a lag between choice of strategy (by random device) and execution, during which it might be "found out" and long enough for counter to be prepared, then this minimum gain will be greater than zero! (this assumes that game is normalized in sense that strats are announced and executed together—but not necessarily chosen at same time).

Note: vN and M could have used notion of mixed strat in connection with minorant and majorant games, getting different results; but they didn't bother to.

A measure of "probable" gains from intelligence--not merely minimum--could be achieved by ruling out "unlikely" (e.g., dominated) enemy strategies, discounting "less likely" ones in advance.

THUS: DON'T MINIMAX REGRET, BUT COMPARE BEST OUTCOME FOR EACH COLUMN WITH THAT OF STRATEGY THAT YOU WOULD USE IN ABSENCE OF AN ESTIMATE OF INTENTIONS: MINIMAX, MAXIMAX, ETC. MINIMUM DIFFERENCE GIVES MINIMUM GAINS FROM PERFECT INTELLIGENCE. IF MAXIMUM DIFFER* ENCE IS SMALL, INTELLIGENCE ISN'T WORTH MUCH.

31. The opponent's perception of the payoff matrix and his consequent intentions may be much less ambiguous than our own estimate of the matrix--i.e., our guess as to the proper counter to the strategy we expect him to use. vN's division of the uncertainties may not correspond to the actual split.

An estimate of intentions requires us to know opponent's view of the payoff matrix (as well as knowing it ourselves).

BUT: the possibility that opponent may me misperceive payoff matrix increases the possibility that intelligence will be valuable--ile., that it will pay to find him out--since it increases the probability that he will be found playing (what we regard as) a lousy strategy (assuming we continue to trust our own estimate). (In non-zero-sum game, there is a chance to change his strategy in our--mutual--favor by "setting him stragith" on payoff matrix; in both zero- and non-zero-sum games it could pay to delude him.)

32. Actual doctrine on counterespionage (CHECK) is to create ambiguity by conflicting indications, not by denying all indications to the enemy (should also have a theory as to what he is likely to do when confronted by this ambiguity).

- 32. The <u>reason</u> vN and M "divide the difficulties" as they do --ambiguity as to opponent's strategy, unambiguous payoff elements--is invalid; it is that they ignore ambiguity that does not arise from game considerations; they assume "nature" behaves probabilistically. If we reject this <u>belief</u> of theirs (they do not present it merely as a convenient assumption), we may conclude that it is not always a convenient assumption.
- 33. LIMITED WAR PROBLEM. Certain strategies have relatively unambiguous (not certain) results. e.g. launching preventive attack; it is virtually certain to evoke retaliation; uncertainties as to number of bombers and missiles we get through, accuracy of bombs, their speed of retaliation, effectiveness of our defenses (which have warning), accuracy of their missiles...may be represented by probabilities.

But other strategies have ambiguous results: e.g. detterrence of various forms, or disarmament; their uncertainties, depending on what Soviets do, are much harder to calculate; the favorable outcomes are much better than the mathematical expectation under the preventive attack (unlike 1948, say) (and for us their worst outcomes aren't much worse; situation is different for Russians, which illustrates usefulness of this analysis), but it is hard to say whether they are more or less likely than other outcomes.

:IA

34. Cigaret ads; filtertips, nicotine and cancer. People buy filtertips on the basis of expectations that they will never be able to check; hence there is no problem to influencing their behavior by creating false expectations. Compare with other expectations that can't be checked, at least until too late: consequences in afterlife; effect on internal organs; influence of internal organs (Carter's Little Liver Pills in both cases); "we could have won last time if..."

Note: expectations in the form of probability distributions may be very resistant to change, especially the more rectangular the distribution. Thus, expectation of a mixed strategy can persist in a repetitive game (Brown; Cournot) where expectation of a pure strategy wouldn't.

35. Possible influences on ambiguity: a) the shape of an "objective" probability dist; between two urns with known distributions, S might act as though the one with the more rectangular distribution were more ambiguous. b) repetition of uniqueness of the choice; S might act as though the "next ball" were ambiguous, but the distribution of the next 1000 balls were not ambiguous (in experiment, might act differently if this we e the "only chance to win" --or "the only chance to lose"--than if he knew he would have many opportunities (not necessarily of the same sort). In each case, check the amounts he would pay for and against an event.

36. Experimental framework. Let A be the amount a subject will pay for the gamble: aAO. (a is an amount constant throughout; say \$10). A is the amount he will pay for OAa; i.e., the maximum amount he will bet "against" A (or on A'). For given a, there will be associated with every event A a vector (A_X, A_Y) .

The Savage axioms imply: for no A,B: $(A_X,A_y) < (B_X,B_y)$

Crucial experiment: find A (ambiguous) and B (unambiguous) for which $A_x < B_x$ and $A_y < B_y$. \bigstar (or vice versa, for wishful thinker.

37. Hypothesis: that perferences among gambles depend on variance as well as mathematical expectation. But this violates Sure-Thing Principle. or admissibility

a) Suppose preference function linear in m.e. and variance, and

positive weight given to variance (risk-taker):

I 1 1 II>I, which violates admissibility II .99.. 1

b) Negative weight to variance (conservative).

I 1 1 1.000..1 I II, which violates

c) Suppose lexicographic ordering: if m.e.'s are the same, negative eight to variance:

I 10 20 III 10 30 I=II, but III < IV, which violates II 20 10 IV 20 20 Milnor's axiom (Rubin? Savage?)

R+Y>B Y+B = R R+ZY > R R+B< 2R

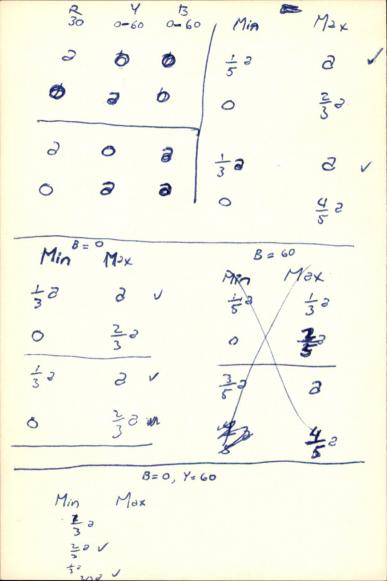
B < 32

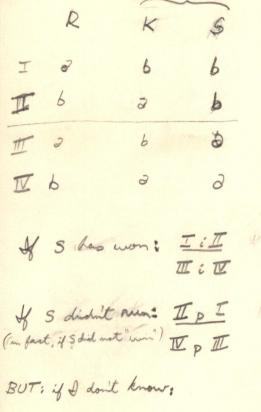
45 45

3

Y=1

Windful Neutral Pess. I i I of 5 has won It I II i IZ TI OTK of sdidn't min TpI IPI IV P II 区户正 Dutknow Ip I IPI I I I I Didn't ma Don't know! Swon Pess III Ip I Ip I ILiV IN THE IN P II Wolfel I i I IPI IPI 世心区 II P IV IV PIL





consultin I, I I PI

R+D and ambiguity

see R-333

How many prototypes should be developed to early test stage? This may depend in the degree of ambiguity we about the results.

(Possible that with subjective probs well-defined, you would never test more than one at at a time). (You must consult yourself on degree of ambiguity)

Again: does rationale for trying "different" solutions ("vulnerable to different uncertainties") really depend on assumption of ambiguity?

R&D as: a) choosing under ambiguity Klein urges them to recognize amb.
b) reducing ambiguity.

Klein urges them to reduce amb.

Two types of wastes: a) acting as though prob were definite, when in fact they are ambiguous. (b) accepting ambiguity, and acting taking it into account, when it is possible reduce it.

Tests vs calculations: reduce ambiguity?

It is not enough to rely on your own feelings of ambiguity, subjective uncertainty, to know when to produce alternative prototypes. Consult record of R&D to know when expectations are "likely" to be contradicted by experience. (Like defining "objective ambiguity" by amount of controversy, difference in predictions; note that Savage designed minimax regret case for just that situation in which there was irreconcilable difference of opinion among respectable consultants—i.e., "objective ambiguity"—almost certainly "subjective ambiguity" so far as the decision—maker were concerned.) (But my people don't minimax regret.) de they?)

Whether or not to pursue two or more parallel lines will depend on immediate cost of doing so, of possible psurprises" (ambiguity) and the importance of the surprises. ((MAY BE QUITE SOUND TO IDENTIFY—as Savage does—SURPRISE WITH THE PRE*EXISTENCE OF AMBIGUITY; this suggests that you should not look at focus outcomes in region where potential surprise is 0, but only when p.s. is positive. Where potential surprise is everywhere 0, maximize expected utility.))

Klein proposes easy rule: do it whenever it is cheap. But harder problem: how long should you keep doing it? Should you do it if it is expensive even in the beginning? Should you stop doing it as soon as it becomes expensive? (This may call for a concept of "degree of ambiguity"; or "potential surprise"?)

Some confusion arising from following fact: a) R&D decisions are designed to reduce uncertainty-risk-ambiguity. (b) R&D decisions are taken, at each stage, under uncertainty-risk-ambiguity. Two theories called for: a) the costs of ambiguity, and how to reduce it; b) how to act given a certain degree of ambiguity.

LEVELS OF AMBIGUITY

15 R, 158 D: 5 R, 50 S: 1R, 18 2) How much to lut, to min \$1

U_T

U_T

D_T

Blood

In theory of statistical inference: is it assumed that the occurrence or non-occurrence of event A gives information only about me the relative likelihoods of A vs. -A?

Or is it possible that it gives information about the relative likelihoods of events that make up -A?

(It appears that in the case of ambiguous events, the latter is true. Knowing that B did not occur, —on the basis of a random draw—gives information about the relative likelihood of R vs. Y

The Zeuthen hypothesis (large differences in critical risk) can simply not be deduced from his assumptions. If it seems plausible, it must be because he (and I) supplies an additional, implicit assumption: perhaps, an assumption on a "typical" degree of uncertainty about opponent's payoffs. or expectations.

My ambiguity hypothesis:

If some events are ambiguous, that then each action has associated with it a range of outcomes, within which probabilities are not assigned. On the other hand, if some events are not ambiguous (say, with respect to each other and to the group of ambituous events), their utilities enter into the range of outcomes weighted by their subjective probabilities. These "constants" will be added to each possible outcome within the range of ambiguity; e.g., they will be The decision would be the same no matter whether: a) subject applies Hurwicz criterion to the ambiguous outcomes, then applies subjective probabilities; or (b) applies s.p. where applicable, then computes max and min for whole action and applies Hurwicz criterion. ((But suppose there are two groups of ambiguous outcomes, with different sp. applied?))

$$\frac{2}{3} + \frac{2}{3}(b - b) = \frac{2}{3} + \frac{2}{3}b$$

$$\frac{2}{3} + \frac{2}{3}(b - a)$$

$$\frac{2}{3} + \frac{2}{3}(b - a)$$

$$\frac{2}{3} + \frac{2}{3}(b - a)$$

$$\frac{2}{3} + \frac{2}{3}(a - a)$$

$$\frac{2}{3} + \frac{2}{3}(a - a)$$

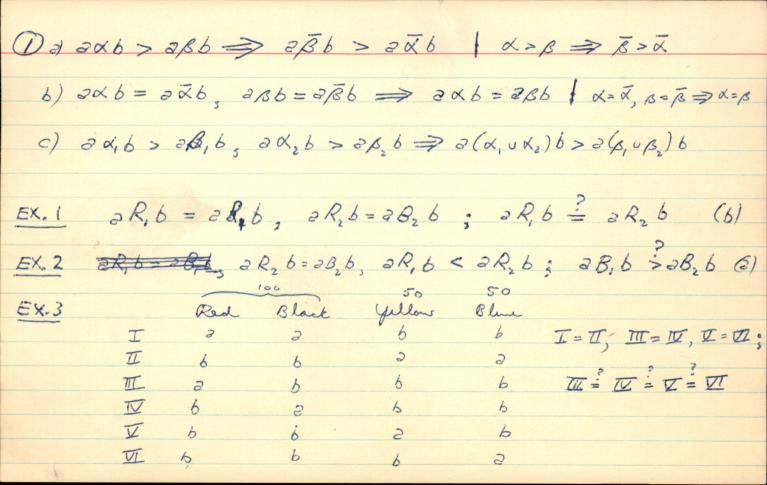
Savage: Knowing that Black is "impossible" (will not come up—as a result of random factors; or did not come up in a random draw) may give knowledge about the relative likelihood of Red and Y ellow. i.e., if information is given that indicates that Black is "less likely" than Red and Yellow together,

given:
$$Y+B=R$$

Suffer: $R+Y>B$ (8"not Josen" in a random draw).

Thus: $R+2Y>R \Rightarrow 2Y>R \Rightarrow Y>R \Rightarrow Y>\frac{R}{2}$ or $Y>\frac{15}{90}$
 $\frac{R}{2}+B<2R \Rightarrow B<\frac{3}{2}R \Rightarrow B<\frac{45}{90}$

(The pount here seems to be that the mere information that "black did not come up" tells more about the relative "likelihood" of Yellow than it does about Red, whose relative likelihood is in some sense "known", and unaffected by the information about the draw.)



Arrow hyp. RYB 1,0,2 1,2,0 2 6 6 b 3 6 2 6 8 6 2 2 1,0,2; R 1,2,0; R 1,0,2; Y 2,0: Y 0,2: B 0,2; B 6 6 2 "Timen B" should have I i II, II i TV "Thirm B" (as would of random draw): $p(X) = \frac{2}{3}$, $p(R) = \frac{1}{3}$, p(B) = 0Lasane R+Y > B; Y+B = 2R given; => Y= R = 1/6, B < 3R = t. (Yor B can be ab 73 or 0).

Suppose & priori $P(B) = f\left(\frac{P_R}{P_o}\right)$ So that if B is "walikely" (wasn't drawn) them \$ R is "probably" > Y. (B(B)) is correlated with $\frac{P_R}{P_r}$; some effects cause Y + B. But if this can't be translated into a priori probe on R, Y, B (i.e. person could have this sort of conditional assumption - and precisely? - and still choose to violate Sure-Thing.)

Arrow: assume both know that appoint knows one's payoffs & expectations. This leads to equilibrium ft. solution - which may require mixed strategies. -1,1 1,-1 1,-1 -1,1 = 1,1 1,10 apon -10,0

10,1 0,0 -1,-1

Talk with Schelling, Aug. 22, 1961

- 1. Consider bets on the proportion of Red to Black in the urn. Schelling assumes that subjects would behave as though subject to Fisher's Uncertainty of Rank B: they would assign probabilities (equal) to the different proportions. But my main proposition is that THEY WOULD TREAT THESE PROPORTIONS AS AMBIGUOUS, WOULD NOT ASSIGN PROBABILITIES TO THEM, although some might be less reasonable than others (if samples had been drawn) and some would be excluded.
- 2. If more than one "best guess," with preservery then the "best guess" distribution can be regarded as the weighted composite distribution corresponding to the mix of these distributions. If the weights added to unity, we would have an overall composite prob distribution. But if they didn't, min and max would apply.

((Another possibility: classes of distributions, ambiguous within class but with weights assigned to each class.))

- 3. ((My evidence is adequate only for inferences about normative rules; though I would hope it had descriptive significance for reflective behavior.))
- 4. ((What I expect to last is: (a) rejection of Savage axioms in situations of ambiguity; (b) influence of "Bad" and "good" possibilities in these situations. Less sure: particular formulal)) ((Question is: do people ask questions about their preferences for payoffs and, separately, about the likelihood of events, the likelihood of these likelihoods, etc...or do they

also ask these questions and also ask what are "good" or "bad" distributions, possibilities? I.e., is their weighting of events in their calculations determined independently of their weighting of payoffs?

Should spell out how formula operates to give weighting of payoffs. Simple cases; complex case.

(INOTEXCEREMENTAXISXASXANDUS)

1. Fillner implies ento, are independent of payoffs, rely only on conf.
2. Does symmetric but reveal proby (Ransay)? Not necessarily.

Shows againstric weight, not probs.
3. Explaint shockle greate; but on "Me will win?" 6-1-1-6

Why the advice to "believe the worst," or weight the unfavorable information in conditions of low information? Why would this have greater survival value, why believe that choosing this way would have results "good enough" to survive or better than some other behavior, unless Nature were really malevolent?

In asking the question, we are implicitly assuming that the available information, it though scanty, is produced "impartially," i.e., independently or randomly distributed with respect to our desires, our payoffs, our set of available actions. But in many situations, we should assume that the information we receive, **EXXEMBER*** (e.g., from subordinates, agents, friendly sources) is already biased in a direction corresponding to our wants; or, they way we perceive or evaluate it is. So that advice would merely tend to counteract this already existing bias in our perceived information. (It is not that Nature is against us, but that our

What can statistician say, in ambiguous situation, when he doesn't know the payoffs (so doesn't know "good" from "bad" distribution)?

He can say about which propositions he would make consistent bets; he might be able to say that he assigned 1/3 probability to Red; perhaps that he assigned x/xx .5 probability to Yellow having at least 1/16 probability.

I.e., he can make probability statements about the proportion of balls in the urn. But where he <u>isn't sure</u> about the probabilities (e.g., of probabilities) he should give us a <u>range</u> of possibilities about which he can make a definite statement (like, attach weight of 95% to proportion's being within this range, 5% to it's being outside it but within this range);

Then we, taking payoffs into account, can attach 95% weight to a Hurwicz maximum within this range, 5% to the Hurwicz maximum outside it, etc.

Typical way to behave; assign equal probabilities in case of ignorance as "best guess" distribution; then "adjust" these, for each act, by raising weight for "bad" outcomes, lowering it for "good," in such a way as to preserve sum of unity. ((Hypothesis: if ordering of outcomes is the same for each act, this should result in the same weights being applied to payoffs for each act.)) Note difference from Fellner, who would apply wwifferm bias to reflecting only confidence, not payoffs.

$$\alpha = \frac{1}{4} \quad \rho = \frac{3}{4}$$
(as though person started with "bust guess" weight, then "breard them" in of the control of the

Gerald Loeb: The present is always the hardest time to invest. In the past there were no uncertainties.

in the present

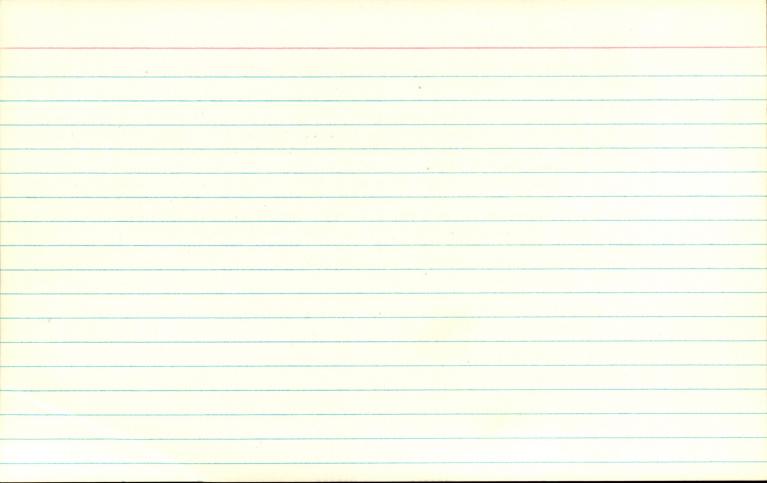
Why is war harder to make choices/to affect the future than to make choices in the present to "affect the past": i.e., hypothetical choices (chosen now) that would "obviously" have affected past and present beneficially if they had been taken in the past.

Obviously, we know more now; have better theories, have more data, new sources of information (diaries, other side's memoirs, etc.); perhaps broader data than available to any one past decision-maker. But that might merely complicate calculations, raise new uncertainties; why in general should it make choice easier, more obvious?

Why isn't choice "easier" and more "obvious" on the basis of less information, partial information?

We try to improve present decision-making by studying past decisions in the light of present information. Tather, like Roberta Wohlstetter, we should try to study past decisions in the light of past information, try to analyze problems of MAKING DECISIONS IN THE PRESENT. In particular, problems of NOISE AND UNCERTAINTY.

Why didn't we more early in (aso? Hyp (su Jaylon): We don't now multanly unites alternature is to lose with certainty. Why? Perhaps: in early stage, who small commitment would wim, other measures also look promising.



Ambiguous strategy is handicapped by double-weighting its less favorable possibilities, versus "traditional" strategy with the same "best estimate" probability distribution and the same outcomes. WHY?

- 1. Suppose one suspects in the case of the ambiguous strategy that one doesn't really know its full range of outcomes, and outcomes could be much worse than one imagines. They could also be better; but if we assume sharply curved utility, we would want to give extra weight to bad possibilities. Hence, giving extra weight to the bad possibilities we can foresee is a way of taking some account of the worse possibilities we have failed to foresee.
- 2. Weighting bad possibilities would be a way of counteracting a wishful bias already suspected to be present in estimates of ambiguous outcomes. If ambiguous strategy is an innovation, its supporters may be especially wishful types; or at least, concerned to stress its good possibilities. Weighting bad possibilities might also be a guard against tendencies to wishfulness.
- 3. You can't explain this by adjusting the utility payoffs of the known outcomes. (a) Even if this worked, it would mean assigning these outcomes different utilities in ambiguous and in risky situations. (b) Utility numbers simply can't be assumed—consistent with assumed ordering—that want will explain certain choices, for any probability numbers. (c) Wouldn't know how to adjust payoffs unless probability numbers are assumed; and they are in question in ambiguous situation.

ambiguous strategy

- 4. Assumption that there are game elements; that opponent (Nature) is really malevolent, and that game is essentially zero-sum.
- 5. Always possibility that this form of behavior is suited to certain situations and is carried over into others by habit, without being really appropriate (e.g., suited to games but carried over into games against Nature).

Chipman and me

Two Russian missiles, same information, to go up first. Taxdemonakrata thairxamusidanaexxRussianaxallamxRrasidankxkoxpiakxSMxmissilexx President controls agent who picks Russian missile. Which does he choose?

(b) a wire is to be used either to heat something, or to act as a safety fuse.

((% MAY BE A FUNCTION OF TH EST, THE "BEST GUESS" EXPECTATION: WHEN THE "BEST GUESS" IS "GOOD" & MAY BE TOW OR O: BUT WHEN THE BEST GUESS IS BAD, & EE MAY BE HIGH. WILL LOOK AS THOUGH PROBS OF AMBIGUOUS EVENT ARE BIASED TOWARD 50:50; but in comparison with a 50:50 unambiguous bet, and may still be less than ½, so that unambiguous bet is preferred. Note that if = ½, the range "best guess" distribution of the ambiguous bet corresponds to the unambiguous distribution of the other bet, and the transpectation with the unambiguous distribution of the other bet, and the transpectation with the distribution with the "best" and "worst" expectations average out to the "best guess" expectation, the subject will be indifferent between the two bets; he may be acting as though they offered the same distribution.

When can probabilities below a certain level be ignored?
When they want could make no difference to our decisions; this will depend on the range of possible payoffs (and, in general, the structure of payoffs).
E.g., if the addition of 1% of the "maximum possible" payoff ranks to the expected value of some action could not affect its ordering—or if we are relatively indifferent between two actions which differ only by that amount—(relative to the effort of taking such possibilities into account) then we might as well ignore probabilities under 1%.

From the desk of . . .

FRAN IRIE

Dan Ellsberg:

TS documents 2114 and 2128 are now available to you in the TS office Room 2783-B. Please come pick them up as soon as possible at your convenience.

Thank you

Fran Drie, alternate TS Officer

HH なへら 0

			22.9	
MESSAGE			DATE 22-9	
to Wan		_	TIME 1:10 A.M.	
DURING YOUR ABSENCE				
mrs. Baum				
of 12-22350 lyt.7				
OF DENELS CLUB NUMBER				
RAND		OUTSIDE		
* PHONED		X	PHONE HIM her.	
WILL PHONE	AGAIN		WANTS TO SEE YOU	
CALLED PERSO	DNALLY		RETURNED YOUR CALL	
MESSAGE:				
M. S. CALLERY				
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FORM 9 (REV. 2-53) BY				

1001 My 1 1 100 2 -88 . 99 reguts show what -1001 you would gain with earious prices of info compand to sayoff to given oction

10 of my decision between I + I is the same if it is true or if it is false, then it should be the saw if I am eventing whithey is to the or faled " This opprious dominance. to not equilent to so go a b b 2 - 6 2 6 6 6 0 6 3 0

With coop, joint max unth side payments To get a one-injutation sol, social, and psychol. assumptions must be added. Now con information leads to mon-coup game, white of ones own matrix (cost of getting conflicte, info too high!

Pene comb. doesn't imply complete info, but equal ignorance - Viner. Firm maximizes some variable in a montolonic relationaly to money. See Dalkey, Economet. Solution - best that do can enforce, with competer information on payoffs. in non-coop, non-commun

4. Advertising is cut down in vacurion: built up windfully in boom, companies don't wally know what it brings in, can't afford to be would in sharp. How explain cut in greatly & shift in contact of add in sharp?

5. Now is period of uncertainty - bell of bean? Pries drift down because no one wants to buy - meadwelle normal sales (not aumound).

Ely drift produced definite expectation of down movement them pressure to sell would develop, accelerate downwing. I

Go Different repretations for "low-prival" and "high-fried" stork.

(8) x. 50R (50B) \$= (3B) ?R 2Kb > 2Bb and 2Kb = CBb (5 CBb)

10R,0 = 12R,0 C28 = 22 b < 2Bb < CBb = 2Kb cmt

10B,0 < 12B,0 [Lut 226 = 2Lb] [Lut 226 - 2Lb]

15. Production decisions may defend on some viducator other than
onis own sales: 2.3. stock market, employment, sales of consume
industry or wail outlets, briess outcome of electrons, federal budgets;
this, expectations which influence decisions some may not be simple
exprepalations of trend of warishless ones own sales.

Some flues are regarded as reasonal; expected, planned for, ignored
(i.e. - do not stimulate new decisions), but unexpected amplitude or
timing (pulops due to coincidence of several "normal" flues) may speen

new decision; while an abound flue may be ignored because it

16. 3am doesn't lave decision model.

comes when a "normal" flue is expected.

17. Notion of SUBJECTIVE DOMINATION - note of expectations in

18. Thread notion of ambiguous weights affected by payoffs - to which minimary or maximax is an appropriation.

19. Instead of regarding economy on a computer, regard it as a set of problem-solving markines, differing in decision-criteria (under unentarity), legs, info networks, ite. Eo. Distriction of Bayes principle"; info may not be "in form of prob. dist "; there, allow randomystion and mixed strategies in stat. division problems and games. E/, application to info theory. 22. Precise stochastic knowledge about the performance of a factor, with egnorance about its total importance, is like knowledge about components but ignorance of

23. May still be possible and useful to measure utility with unambiguous wents,

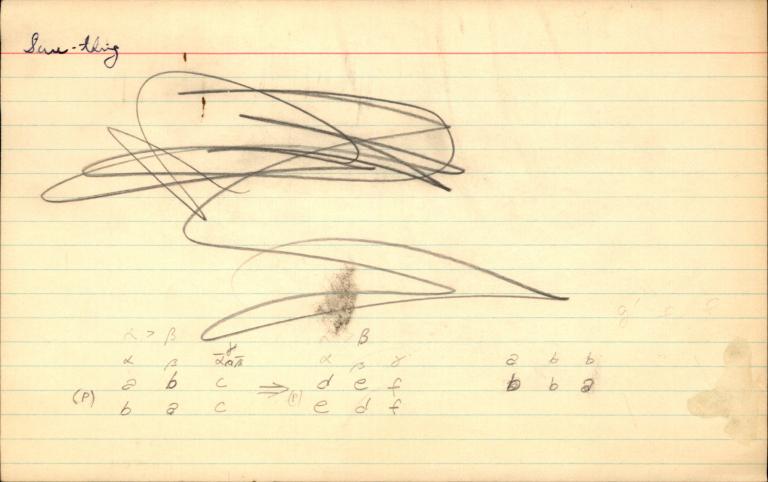
24. Uncertainty in decision group decision - moting of wilfare te.

7

27. Degre of preference will influence ; 3) the ranking of party platforms by a voter (other than his preferred platform platform in sense of a ranking of goals, not muly a set of simultaneous objectives). -> b) the framing of a platform by party : when the relative undesirability of an uncongenial plant is weight against the probable support it will bring (met) and the probable effect of this support on the election (i.e., whith or not it is "probably" note: election represents a level of achievement type good. Multi-step good: promotion in school or bureaucratic hirarchy. brussing-sty goals; yardsge in a football game (10-yal interes). military campaigns. See Kaplan on (Military Worth) success functions. These amount to specific assumptions on preference maps : possibly worful if they correspond to important classes (not menely individuals); they verginging differences, they take advantage of similarities. On median hurdle (sound benier) case: shifting classes.

28. Consept of "reasonable doubt"; defendent on valuation of Type I and Type II wood - not just a doubt "equal to" / in 1000, say. 29. Military estimate of "intentions" Vs. "capabilities." Problem is to estimate intentions, but allows for their ambiguity. (and for ambiguity of other factors).

NOTE: in wal game, ambiguity of payoff ilements may be much In greater than of apponents intentions. NOTE: gains from knowledge of intentions may be much queter I than gains from mixed "oftimal" strat ers. Sure "non optimal" strat. This is test whither it is morthwhile to reduce spraifie ambiguities. 30. Why are do closed and investment cos sullet a discout from court votre? Where the "value" is below the "level of expiration" (e.g. total annihilation but not object") there is greater pressure to estimate intentions - and influence them. Can we (or "X" country) afford to be conservative (or wishful), gue on level of aspiration.



of $\alpha = \frac{1}{2}$, the state of any $\beta \neq \frac{1}{2}$, $\beta > \alpha > \beta$ or $\beta > \alpha > \beta$ which means if X is any went was - 1 , then for any B + 1, with the let (at some odds) on B on on B. e.g. die nid from um with unknown natio. must exten prefer Red at of this um to Red out of um with known ratio (kg. 49R-51B) and (Street) of Ruis despend to Rx p% of the time, Bx must be knowed to Ry same P%.

You are an Astronaut, You are in charge of picking, for each flight, whether an Atlas or a Titan will be used as booster. Each has had an observed reliability of .6; the Atlas has had 100 tests, the Titan 25. So with 95% confidence, the reliability of the Atlast is over .51, the reliability of the Titan is over .41. With 95% conf., the prob. that the Atlas will abort is...

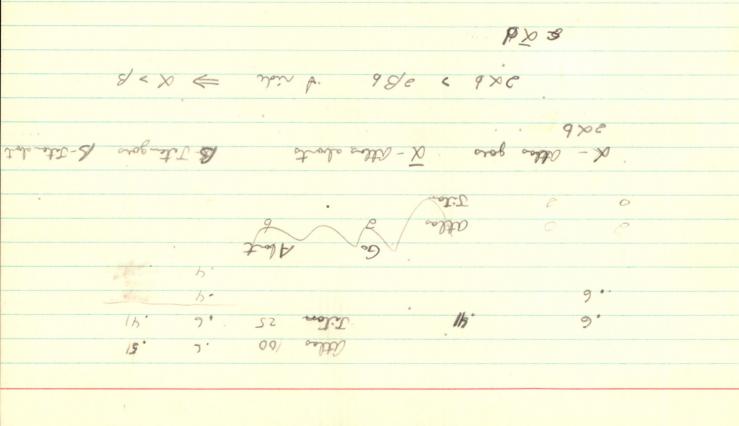
Your own flight will be second. Your worst enemy is shheduled to go first. If his missile doesn't abort, he will be first Man in Space. Which missile do you give him?

(b) Before you know results of his attempt, you must pick your own missile. Which do you pick?

(Conservative: pick Atlas for both. Can't be as confident that the Titan will abort; or that it will <u>not</u> abort. Yet this means you act "as if" you felt that Titan were "more likely" to abort, and also that it is "more likely" to succeed.)

Wishful: pick Titan for both.

Yet some will pick Titan for enemy, Atlas for self.



John Cohen a hark Hansel: Risk and Sambling, the Shits of Subjective Probability Lagrend fren a Col London 1956.) (Prof + Lent of Prycholog, Unin of humchester) articles by farreth-Koodnow in am. four. of Psychol. + Jour. of Exp. Psychol., 1955-56 Ray Hyman, same, 1955-56 Preston + Baratta, "auction Value of an Uncertain Outer ANP or UXP Chipman: Stochastic Choice and Subjective Probability

Notion that an individual in a given "state of mind" will be considered as having a strong ordering of the elements of the choice set, but that he has a prob dist over all possible statesof mind (i.e. permutations of the choice set). Assume finite set.

Ramsey's notion of "ethoically neutral event"; if the preference of xAy over yAx is independent of the particular x and y, provided that one is absolutely preferred to the other. "This implies that the outcome of the event A is not itself an object of desire which would influence one's choice between x and y." p. 3 "Since our findamental notion is that of a prob dist over states of mind, we can say that if P(x,y) equals 1, then $\mathbb{R}(x \pm x \pm x) + P(x' \times y', y' \times x') = P(x \times y, y \times x)$, given P(x,y')=1.

"The justification for the assumption of 'ethical neutrality' of beliefs is that one should be able to find a sufficiently interesting set E of events the outcomes of which are not themselves the objects of desire. It is plain, however, that if we are to include events such as 'Nixon will be the next president.' the assumption will no longer be warranted." 4

((But Chipman ignores possibility of reverse influence; events desirability being influenced by the payoffs -- perhaps in some other

gamble.))

Chipman . 2. Savage: if x is preferred absolutely to y. (P(x, y)=1), (xxy) p (xBy) > x is subjectively more probable than S. of Q(K, B) is the (objective) prob that X is considered more blug than B, then Q(K, B) = P(0, b). Likewise, for those states of mind in which y is preferred to x, preference of a over b -> B is considered more probable than & X, so Q(B, X) = P(3, 6). Sime P(x, y) is the prob of the first state of mind and P(y, x) the second, P(a,b) = P(x,y)Q(x,B) + P(y,x)Q(B,x)which is duce's decomposition axiom. L Note: if P(x, y) = 1, P(y, x) = 0, then Q(x, B) = P(0, 6). Since Q is suffered to be independent of the payoffs, it should be the same for all payoffs, defending only on & and B. But minimager: (2 & b) p (2 B b) for small 3, 6; but with ambiguous &, B and large 3, b, Q(x, B) = P(x, y) may be close to z ; in the limit, = z , so that small increments (to b, say) could swing perference with way). P(x, y) + P(a, b) - 1Q(x,B)= 2 P (x, y) -1

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Weak transitivity postulate:

For all 3, 6, c & A, if P(3, 6) \geq \frac{1}{2}, \text{thin p} and P(6, c) \geq \frac{1}{2},

then P(3, c) \geq min [P(3, 6), P(6, c)]

(stranger than Marselak + Davidson week part. that P(3, c) \geq \frac{1}{2})

Strong trans. post:

For all 3, b, c $\in A$, if $P(3,b) \ge \frac{1}{2}$ and $P(b,c) \ge \frac{1}{2}$ thin $P(b,c) \ge Max [P(b,b), P(b,c)]$ This is some as $M \ne 0$'s strong trans. post.

But suppose: & is drawing ball from with Exp in duce.

Experiment: S chose between matchboxes, some of which contained a given proporition of heads and stems (60-40, 50-50, etc.), and some with unknown proporitions: but samples (7-3, 4-6, etc.) were drawn from the latter. Money bets. (three wagers: 25,-25; 0-25; 0, 25)

Results: 1. Between boxes with known dists, subjects always

chose the better dist.

2. Ss violated the Strong Transitivity Post (Marschak and Davidson). i.e., the proporition of perference of a over c was less than the maximum of a over b or b over c (latter might be 1).

All subjects conformed, to reak trans postulate.

4. Much violation of Luce's linearity axiom: that for all a,b in A, either P(a,c) greater or equal to P(b,c) for all c in A, or less than or equal.

5. Same individuals violated Luce's Independence of Irrelevant

Alternatives axiom.

6. "One of the most striking features shown by the data is the tendency for individuals to bias unknown probabilities towards one-half." 22 I.e., where sample shows 7 heads, 3 tails, subject prefers box with known 70-30 dist; but where sample shows 3 heads, 7 tails, subject prefers that unknown box to one with known 30-70 dist.

Subjects strongly preferred a known 50-50 dist to an unknown dist with a 5-5 sample.

((The preference when math. expect is negative conforms to wishful

thinking; but behavior under high favorable probs doesn't. But maybe wishful thinking operates strongly (or only) when the problem is to avoid a loss. Or, perhaps these preferences depend on the scale of payoffs; perhaps with larger scale, subjects would have shown consistently wishful thinking.

Or, it may not show wishful thinking; choices suggest a Bayesian principle at work, assigning uniform probs to unknown events; except that they preferred 50-50 to 5-5 sample. Exp: Which theyxxw would they prefer, a 50-50 box or a box with completely unknown dist, no sample

drawn? This would be a direct test of Bayesian hypothesis.

Kaysen suggests a preference for higher variance? Is there any basis for saying that the unknown box has a higher variance? I don't think so. Anyway, we could test directly by seeing if subject preferred a box with a higher known variance to a box with a lower known variance, or with unknown variance (I think we must say that sample box has unknown variance; all we have is a maximum likelihood estimate of the mathematical expectation). ((((())))))

((((EUREKA: Doesn't Luce independence of probs and utilities imply: $(a \times b)i(b \times a)$ $(a \times b)i(b \times a)i(b \times a$ This experiment is counter-example. With 5-5 sample, subjects would be indifferent betwen betting on heads or stems; but they would prefer to draw from a box with a known 50-50 dist. In fact, they might prefer to draw from a 49-51 box, though this wasn't tested.)))

a-50% from dist 8-50-50 scape

i.e. (2xb) ((bx2), (2Bb)(bp2), BUT 2 (2xb) p (2Bb)

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??Did these preferences between known-unknown dists hold for negative, positive and pro math expectations? Or was there a difference? Would they be the same for different levels of payoff?

Chipman mentions that the data on thes pair "suggest that a minmax

principle is at work."

Chipman concludes that subject does not merely characterize event by a probability, but that some other parameter is involved; he concludes that the other parameter is sample size (i.e., size of sample drawn from unknown dist). ((My opinion: the other parameter is somethinglike confidence or ambiguity, with perhaps a third parameter of importance. Sample size is an indicator of confidence and ambiguity, but not always applicable, rarely well-defined).))

"Our basic approach has been that, whether the subject is conscious of it or not, he acts as if any event could be characterized by two numbers, one of them a frequency and the other a sample size." "For example the casual poker player will not bother to figure out, in a game of five-card stud, whether the objective probability (in the conventional sense) of playing for a straight is higher than that of playing for a full house; NE...In the samplest case, we may say that he simply observes how many times he won or lost when he previously faced this alternative, and acts according to the observed frequency and sample size." ((NOTE: C. fails to say that he

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acts according to the frequencies he has previously observed to occur, but according to his previous wins and losses. This is probably true; subject is influenced by his wins and losses, though Chipman generally hints that he is influenced only by his observations))

In any case, "the scientist has no choice but to discover the

subject's theory in order to predict his behavior."

((Counter-Luce: suppose minimax behavior consisted not in acting as though worst outcome were certain, but as though it was more probably than otherwise, depending on importance. A strict minimaxer, will be indifferent between all gambles offering the same outcomes, whatever the events; i.e., P(a,b) will always be 1/2, where a and b are gambles offering the same outcomes. But a p quasi-minimaxer, abover will approach indifference, as the payoffs get larger (Chipman's exp. suggests-as they get negatively large, between gambles involving same payoffs and ambiguous events; thus

SUBJECT CAN BE SAID TO ACT AS IF HE ATTACHED PROBABILITIES TO PAYOFFS, NOT EVENTS (in the limit); i.e., payoffx gets a weight (which need not equal 1--Hurwicz) which depends only on its relative size.